

## CONDITIONS & PROBABILITIES



P(H)

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## CONDITIONAL PROBABILITY

probabilities really are conditioned on information

$P(j | k) = n_{j \text{ and } k} / n_k$   
read as 'Probability for j given k'

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if two dice are tossed, then a convenient graphical analysis may be used to calculate ns

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$$P(j | k) = n_{j \text{ and } k} / n_k$$

**P(7 or 9 sum | second die yields 2 or 3)**

$$n_{7 \text{ or } 9 \text{ and second die yields 2 or 3}} = 3$$

$$n_{\text{second die yields 2 or 3}} = 12$$

$$P(7 \text{ or } 9 \text{ sum | second die yields 2 or 3}) = 3 / 12 = 1 / 4$$

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$$P(j | k) = n_{j \text{ and } k} / n_k$$

$$= (n_{j \text{ and } k} / n) / (n_k / n)$$

$$= P(j \text{ and } k) / P(k) = (1 / 12) / (1 / 3)$$

if j and k are independent, then the  
unconditioned multiplication rule is  
recovered

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## GENERAL PROBABILITY RULES

$$P(j \text{ and } k) = P(j | k) P(k)$$

$$P(j \text{ or } k) = P(j) + P(k) - P(j \text{ and } k)$$

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